

FACULTY OF ENGINEERING
B.E. 2/4 (CSE) I- Semester (Suppl.) Examination, July 2014

Subject : Discrete Structure

Time : 3 Hours

Max. Marks: 75

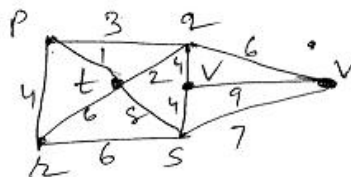
Note: Answer all questions of Part - A and answer any five questions from Part-B.

PART – A (25 Marks)

- 1 State Demorgan's law.
- 2 Write the logical equivalence to $p \vee (7P \wedge q) \rightarrow (p \wedge q)$
- 3 List the properties of Pigeon hole principle
- 4 Given set $p = \{1, 2, 3, \dots, 7\}$. How many symmetric relations are there on p.
- 5 Define surjective function. Write a surjective relation in for given set $A = \{1, 2, 3, 4, 5\}$
- 6 Define semigroup and monoid.
- 7 What is non homogeneous recurrence relation? Give one example.
- 8 Write the properties of algebraic system.
- 9 Solve the Recurrence Relation $a_n - 13a_{n-1} + 42a_{n-2} = 2^n$
- 10 Find chromatic Number of a Bipartiate graph.

PART – B (50 Marks)

- 11 (a) Define Tautology. Verify $[7r \rightarrow 7(pvq)] \rightarrow [(pvq) \rightarrow r]$ is Tautology or not.
 (b) Show that $p \oplus q$ is equivalent to $(p \wedge 7q) \vee (7p \wedge q)$
- 12 (a) Prove that $A \cup (B \cap C) = (A \cup B) \cap (A \cup C)$
 (b) The function $f : \mathbb{R} \rightarrow \mathbb{R}$ defined as $f(x) = \begin{cases} 3x - 5; & x > 0 \\ -3x + 1; & x \leq 0 \end{cases}$ Then determine
 (i) $f(-1)$, $f(2/3)$, and $f(-2/3)$ (ii) $f^{-1}(0)$, $f^{-1}(-6)$, $f^{-1}(1)$
- 13 (a) List and explain the properties of Binary relations with example.
 (b) State and explain the principle of inclusion and exclusion.
- 14 (a) Solve the recurrence relation
 $a_n - 9a_{n-1} + 26a_{n-2} - 24a_{n-3} = 0$ for $n \geq 3$ where $a_0 = 0$; $a_1 = 1$; $a_2 = 10$
 (b) Solve the RR $a_r = 3a_{r-1} + 2$; $r \geq 1$, $a_0 = 1$
- 15 (a) Find the coefficient of x^{15} in $\frac{(1-x)^4}{(1+x^4)}$
 (b) Write short note on Group code and its applications.
- 16 (a) Prove that $\langle \mathbb{Q}^+, * \rangle$ is an algebraic system and $*$ is a binary operator on \mathbb{Q}^+ is defined by
 $a * b = \frac{a \cdot b}{5}$ is a group.
 (b) Define Hamitanian graph write the basic rules for constructing this graph.
- 17 (a) Define minimal cost spanning Tree. Use Kruskal's algorithm to determine the minimal cost spanning Tree for the following graph.



- (b) Define chromatic number. Find the chromatic number for the graph above Question (i.e.17(a)).
