

CONCEPTS OF PLANES

Planes are 2-D closed figures. In our subject, planes are closed polygons like triangle, square, rhombus, pentagon, hexagon, circle and semi circle. **TV**

Projections of planes means drawing the front view, top views and sometimes, side views.

Always remember, in one view, the projection of plane is the true shape and in other view, it is a line.

- 1) **FV** → **True shape**
TV → **Line**
- 2) **TV** → **True shape**
FV → **Line**

Hence the problems on planes simply involves **FV** deciding where to draw the shape. If this is decided correctly, the other view is a line. Hence most important concept in planes is to decide where the shape is to be drawn.

There are 3 cases of planes problems. They are as follows:

- 1) Planes Parallel to HP or VP (1 stage)
- 2) Planes inclined to HP or VP (2 stages)
- 3) Planes inclined to both HP & VP (3 stages).

Planes are also called as surfaces or lamina.

Edge & Corner concept:

If an **edge** is in **HP** or **VP**, the **starting side** of the polygon is **vertical**.

If **corner** is in **HP** or **VP**, the **starting side** should be **horizontal**.

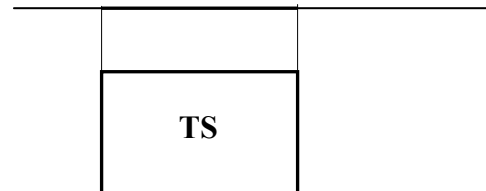
For a **Square**, **Corner** means **sides** at 45° to the x-y line.

If edge is \parallel to HP or VP, it is a horizontal

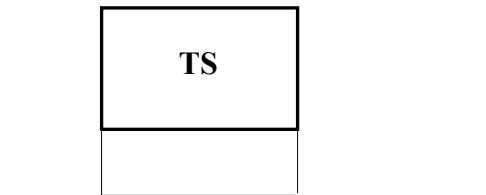
If edge is \perp to HP or VP, it is vertical.

Case 1) Planes or surfaces \parallel to HP/VP**a) Planes \parallel to HP (\perp to VP)**

TV → **True shape**
FV → **Line**

**b) Planes \parallel to VP (\perp to HP)**

FV → **True shape**
TV → **Line**

Simple rule

Plane \parallel to HP → shape w.r.t VP (TV)

Plane \parallel to VP → shape w.r.t HP (FV)

In this case, following data to be noted:

- 1) Shape of plane
- 2) Plane \parallel to HP/VP (where to draw shape)
- 3) Edge(side)/ Corner in HP/VP or Side inclined to HP/VP (for starting side)

12.2) An equilateral triangle of 50 mm sides has its plane parallel to HP and 25 mm above xy. Draw its projections if one of its sides is inclined at 45° to the VP.

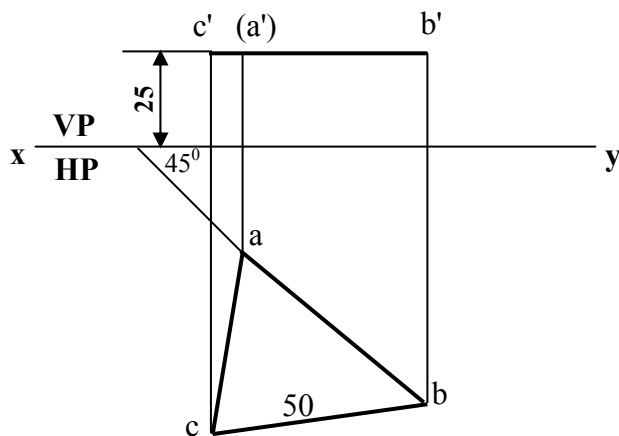
Ans) Given data:

Shape \longrightarrow triangle (all 50 mm sides)
 Plane \longrightarrow \parallel to HP (**Shape** w.r.t.VP)
 Side/ Corner \longrightarrow Side angle at 45°

Logic: Since the plane is \parallel to HP, shape is w.r.t VP (Top View) and line is in FV.

Steps:

- 1) Draw a side of \blacktriangle at 45° below xy.
- 2) Cut arcs from a & b to get c. Join abc.
- 3) Project lines from a, b & c to get line a'b'c' (FV) at 25 mm above xy line.



Note: From Projection of Planes onwards, we have to show the position of reference planes (VP & HP) with respect to x-y line.

Always note that VP is above x-y line and HP is shown below x-y for the First Angle Projection.

12.3) A square of 40 mm has a corner in HP and 20 mm in front of VP. All sides of the square are equally inclined to HP and \parallel to VP. Draw its projections.

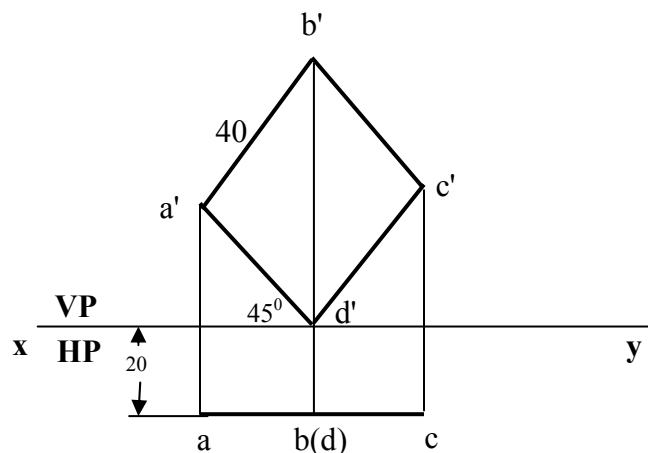
Ans) Given data:

Shape \longrightarrow Square of 40 mm
 Plane \longrightarrow \parallel to VP (shape in TV)
 Side/ Corner \longrightarrow Corner (45° sides)

Logic: Since the plane is \parallel to VP, shape is w.r.t HP (Front View) and line is in TV.

Steps:

- 1) Draw a square a'b'c'd' of 40 mm at 45° in FV, with a corner touching x-y.
- 2) Project lines from a'b'c'd' to get line abcd (TV) at 20 mm below x-y.

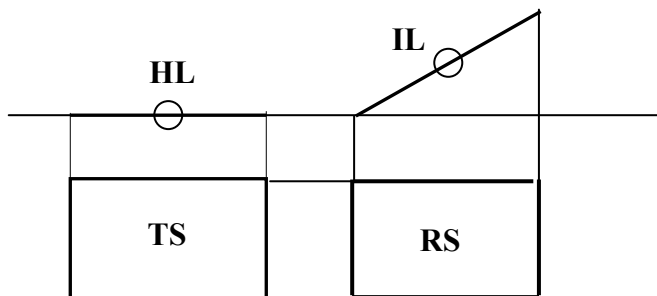


Case 2) Planes (surfaces) inclined to HP /VP

When planes are inclined to HP or VP, then its reduced shape will be seen in the opposite view.

a) Planes (surfaces) inclined to HP (\perp to VP)

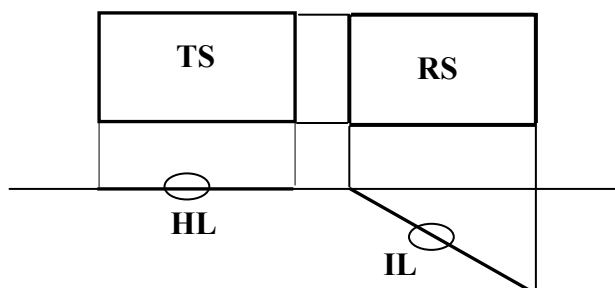
TV \rightarrow Reduced shape (RS)
FV \rightarrow Inclined Line (IL)

**Note:**

- 1) The **Inclined line (IL)** is of same length as the **Horizontal line (HL)**. Only angle changes in 2nd stage.
- 2) **Projectors** from **Inclined line (IL)** and **TS** gives the **Reduced Shape (RS)**

b) Planes (surfaces) inclined to VP (\perp to HP)

FV \rightarrow Reduced shape (RS)
TV \rightarrow Inclined Line (IL)

**Simple rule**

Plane Inclined to HP \rightarrow RS w.r.t VP (TV)

Plane Inclined to VP \rightarrow RS w.r.t HP (FV)

In this case, following data to be noted:

- 1) Shape of plane
- 2) Plane \perp to HP/VP (where to draw shape)
- 3) Edge(side)/ Corner in HP/VP (For starting side)

Steps to solve problems on Inclined planes:

- 1) Assume that plane is parallel & draw TS & HL in 1st stage.
- 2) Draw IL and then get RS in 2nd stage.

Note: the following abbreviations will be used throughout the topic to make it easier for understanding.

TS: \rightarrow True shape.
RS: \rightarrow Reduced Shape.
HL: \rightarrow Horizontal Line (Projection of TS)
IL: \rightarrow Inclined Line (Plane angle; Length is same as HL).
FV: \rightarrow Front View (Drawn above xy line)
TV: \rightarrow Top View (Drawn below xy line).

12.4) A regular pentagon of 25 mm sides has a side on the ground. Its plane is inclined at 45° to HP & \perp to VP. Draw its projections.

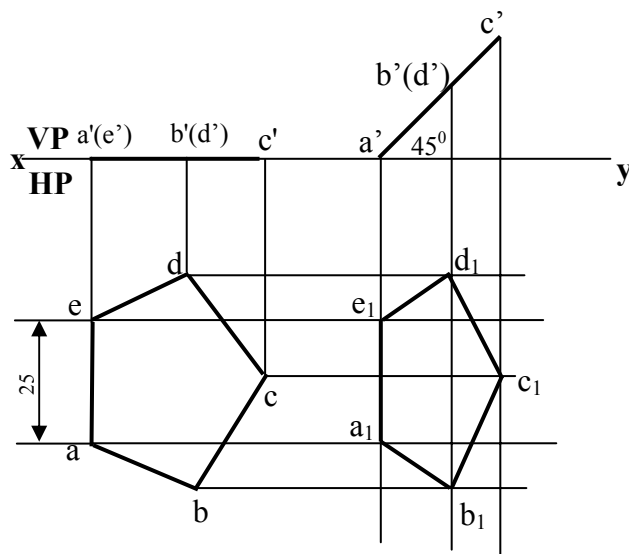
Ans) Given data:

Shape \longrightarrow Pentagon (25 mm sides/ 108°)
 Plane Angle \longrightarrow HP (Red' Shape w.r.t.VP)
 Side/ Corner \longrightarrow Side (starting side vertical)

Logic: Since the plane is inclined to HP, Reduced shape (RS) is w.r.t VP (Top View) and Inclined line (IL) is w.r.t HP (FV).

Steps:

- 1) In TV, draw pentagon (TS) abcde of 25 mm with starting side vertical & HL a'b'c'd'e' on xy.
- 2) In 2nd stage, at 45° draw IL a'b'c'd'e' of same length as HL and mark points at same distances on IL as in HL.
- 3) Project lines from all points of IL and from TS to get the RS a₁b₁c₁d₁e₁.



12.5) Draw the projections of a circle of 50 mm diameter having its plane vertical and inclined at 30° to VP. Its centre is 30 mm above HP and 20 mm in front of VP.

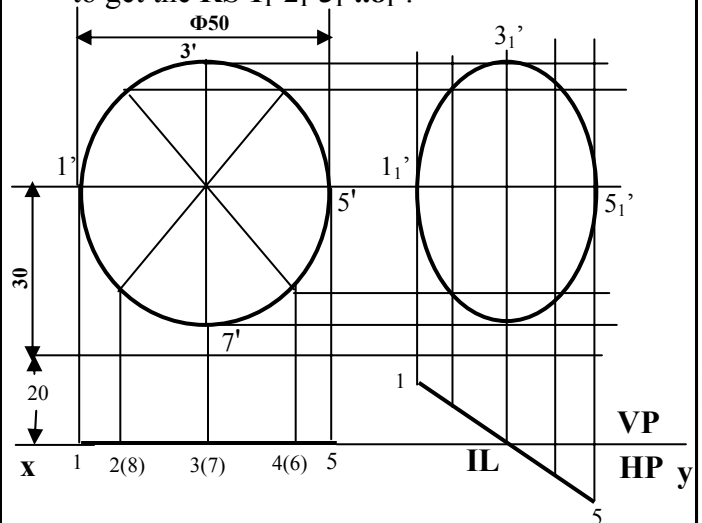
Ans) Given data:

Shape \longrightarrow Circle 50 mm diam.
 Plane Angle \longrightarrow VP (RS w.r.t HP)
 Side/ Corner \longrightarrow Not needed.

Logic: Since the plane is inclined to VP, the RS is w.r.t HP (FV) and IL is w.r.t VP(TV).

Steps:

- 1) In FV, draw a circle (TS) of 25 mm radius with centre 30 mm above xy and HL at 20 mm below xy. Divide circle into 8 parts 1',2',3'....8'
- 2) In 2nd stage, at 30° , draw IL 1-2-3.. of same length as HL and mark points at same distances on IL as in HL.
- 3) Project lines from 1-2-3-4.. of IL and from TS to get the RS 1₁'2₁'3₁'..8₁'.



Case 3) Inclined to both HP & VP.

In this case, **Plane (surface)** is inclined to **HP/VP** and **Reduced Shape (Side/Diagonal/Diameter)** is inclined to **VP/HP** and vice versa.

These problems are solved in 3 stages.

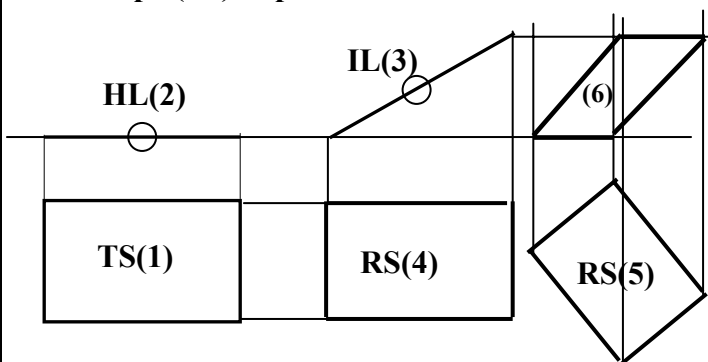
1) Solve the problem using **Plane angle** method and get the **1st & 2nd** stages.

2) In the **3rd** stage, turn the **Reduced shape** (by its **side/diagonal/diameter**) by the **given angle** and then its **projections** are **matched point to point** to get the **final shape** of the **plane**.

In total, there will be **6 figures** to be drawn, **3 in FV** and **3 in TV**.

a) Planes (surfaces) inclined to HP (\perp to VP) & shape (side/ diagonal/ diameter) inclined to VP

- 1) TV \rightarrow **Reduced shape (RS)**
- 2) FV \rightarrow **Inclined Line (IL)**
- 3) TV \rightarrow **Turn the RS at given angle and redraw it, using arcs.**
- 4) FV \rightarrow **Draw projections now and match point to point from IL to get final shape (FS) of plane in FV.**

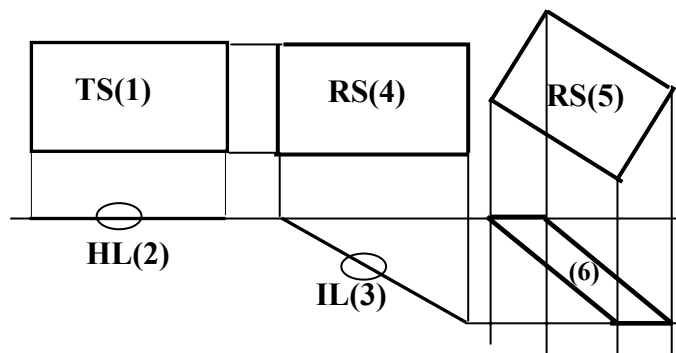


Note:

The **RS (5)** should be turned about the side which is **vertical or horizontal**.

b) Planes (surfaces) inclined to VP (\perp to HP) & shape (side/ diagonal/ diameter) inclined to HP

- 1) FV \rightarrow **Reduced shape (RS)**
- 2) TV \rightarrow **Inclined Line (IL)**
- 3) FV \rightarrow **Turn the RS at given angle and redraw it, using arcs.**
- 4) TV \rightarrow **Draw projections now and match point to point from IL to get final shape (FS) of plane in FV.**



Simple rule

Plane Inclined to HP \rightarrow RS w.r.t VP (TV)
Plane Inclined to VP \rightarrow RS w.r.t HP (FV)

In this case, following data to be noted:

- 1) Shape of plane
- 2) Plane le to HP/VP (where to draw shape)
- 3) Edge (side) / Corner in HP/VP.
(1st and 2nd stage will be over here)
- 4) Shape angle VP/HP (side/diagonal/diam)

Steps to solve problems on Inclined planes:

- 1) Assume that plane is parallel & draw TS & HL in 1st stage.
- 2) Draw IL and then get RS in 2nd stage.
- 3) Turn the RS in the 3rd stage and match projections from IL to get Final shape.

12.6) A square ABCD of 50 mm sides has its corner A in HP; its diagonal AC is inclined at 30° to HP & diagonal BD at 45° to VP & \parallel to HP. Draw its projections.

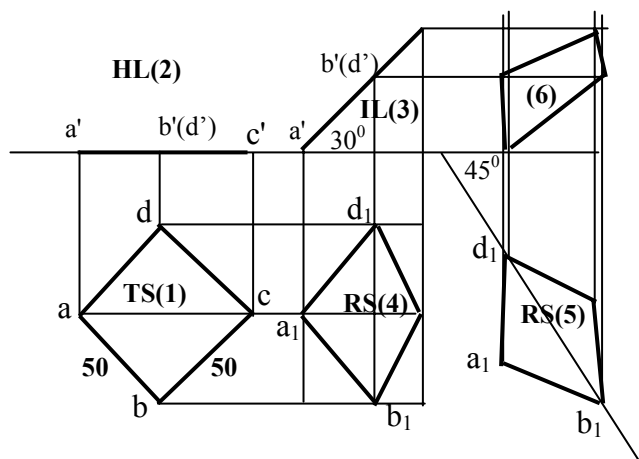
Ans) Given data:

Shape \longrightarrow Square (50 mm sides)
 Plane Angle \longrightarrow 30° to HP(AC)
 Side/ Corner \longrightarrow Corner (sides at 45°)
 Shape angle \longrightarrow Diagonal at 45° to VP(BD)

Logic: For squares and rhombus, if plane angles are not mentioned, then the diagonal angles are treated as plane angles and shape angles. In this problem, AC is treated as **Plane angle** and BD is treated as **shape angle**. **Reduced shape (RS)** is w.r.t VP (**Top View**) and **Inclined line (IL)** is w.r.t HP (**FV**).

Steps:

- 1) In 1st stage, in TV, draw square (TS) abcd of 50 mm with starting side at 45° & HL a'b'c'd' on xy.
- 2) In 2nd stage, at 30° draw IL a'b'c'd' of same length as HL and get the RS by projections.
- 3) In 3rd stage Rotate b₁d₁ at 45° to VP and draw RS. Take projections up and match point to point from IL to get Final Shape a₁'b₁'c₁'d₁'.



12.8) Draw the projections of a circle of 50 mm diameter having its plane angle at 45° to HP & its top view of diameter makes an angle of 30° to VP.

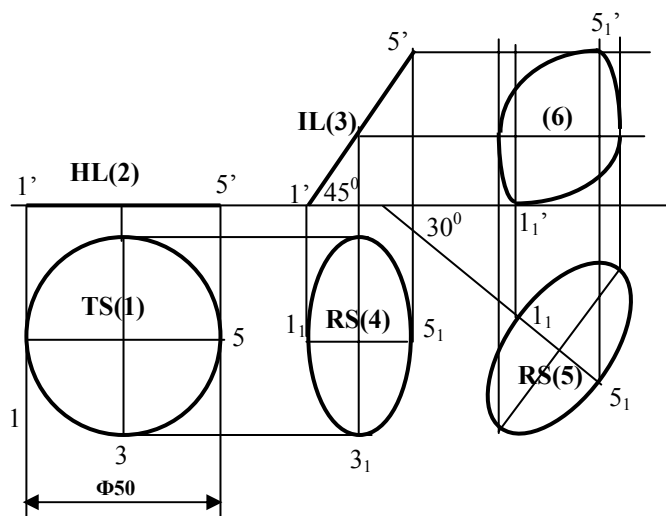
Ans) Given data:

Shape \longrightarrow Circle 50 mm diam.
 Plane Angle \longrightarrow 45° to HP (RS in TV)
 Side/ Corner \longrightarrow Not needed.
 Shape angle \longrightarrow Diameter at 30° to VP

Logic: Since the plane is inclined to HP, the RS is w.r.t VP (TV) and IL is w.r.t HP (FV). In the 3rd stage, turn the RS about diameter by 30° and match projections above to get final shape.

Steps:

- 1) In 1st stage, in TV, draw a circle (TS) of 25 mm radius below xy and HL 1'.2'..8' on xy. Divide circle into 8 parts 1,2...8.
- 2) In 2nd stage, at 45° , draw IL 1'.2'..8' of same length as HL and get RS by projections.
- 3) In 3rd stage, rotate 1₁-5₁ by 45° to VP and draw RS. Take projections up and match point to point from IL to get Final Shape 1₁'2₁'..8₁'.



Exercise Problems:

2) A regular hexagon of 40mm sides has a corner on HP. Its surface is inclined at 45° to HP & the top view of the diagonal through the corner which is in HP makes an angle of 60° with VP. Draw its projections.

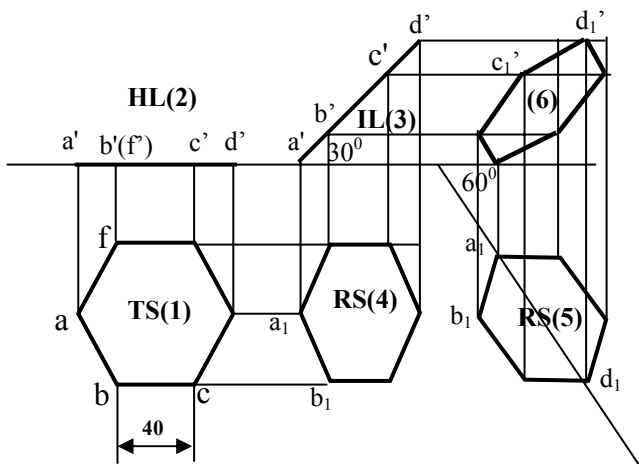
Ans) Given data:

Shape \longrightarrow Hexagon (40 mm/120⁰ sides)
 Plane Angle \longrightarrow 45° to HP (RS in TV)
 Side/ Corner \longrightarrow Corner (side horizontal)
 Shape angle \longrightarrow Diagonal at 60° to VP

Logic: Since the plane is inclined to HP, the RS is w.r.t VP (TV) and IL is w.r.t HP (FV). In the 3rd stage, turn the RS about diagonal by 60° and match projections above to get final shape.

Steps:

- 1) In 1st stage, in TV, draw hexagon (TS) abcdef of 40 mm with starting side horizontal & HL a'b'c'd'e'f' on xy.
- 2) In 2nd stage, at 45° draw IL a'b..f' of same length as HL and get the RS by projections.
- 3) In 3rd stage Rotate a₁d₁ at 60° to VP and draw RS. Take projections up and match point to point from IL to get Final Shape a₁'b₁..f₁'.



7) A semi circular plate of 80 mm diameter has its straight edge in the VP and inclined at 45° to HP. The surface of the plate makes an angle of 30° to VP. Draw its projections.

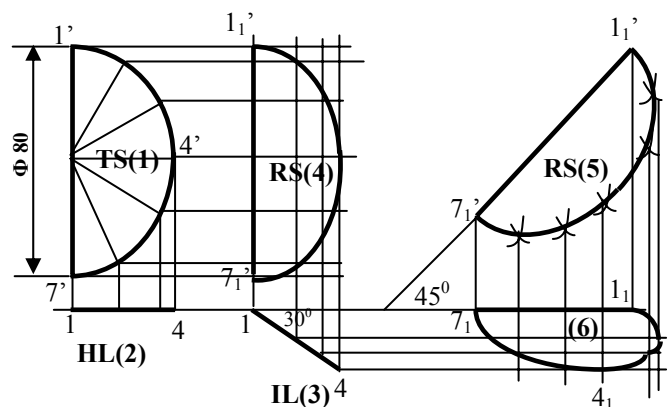
Ans) Given data:

Shape \longrightarrow Semi circle, 80 mm.
 Plane Angle \longrightarrow 30° to VP (RS in FV)
 Side/ Corner \longrightarrow Edge (side vertical)
 Shape angle \longrightarrow Side at 45° to HP

Logic: Since the plane is inclined to VP, the RS is w.r.t HP (FV) and IL is w.r.t VP (TV). In the 3rd stage, turn the RS about side by 45° and match projections below to get final shape.

Steps:

- 1) In 1st stage, in FV, draw a semi circle (TS) of 40 mm radius above xy with starting side vertical and HL 1.2..7 on xy. Divide semi circle into equal parts 1,2...7.(30° each).
- 2) In 2nd stage, at 30° , draw IL 1.2..4 of same length as HL and get RS by projections.
- 3) In 3rd stage, rotate 1'-7' by 45° to HP and draw RS. Take projections below and match point to point from IL to get Final Shape 1₁2₁..7₁.



Exercise Problems:

9) A plate having the shape of an isosceles triangle has base 50 mm and altitude 80 mm. It is so placed that in the front view it is seen as an equilateral triangle of 50 mm sides and one side inclined at 45° to xy. Draw its top view.

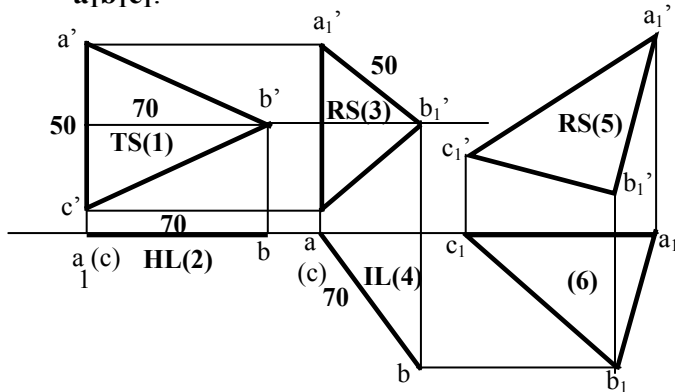
Ans) Given data:

- True Shape \longrightarrow Isosceles \blacktriangleright (50/80)
- Red Shape \longrightarrow Equilateral \blacktriangleright (50)
- Side/ Corner \longrightarrow Side (Start side Vertical)
- Shape angle \longrightarrow Side at 45° to VP
- Shape change \longrightarrow Front View
- \implies Plane Angle \longrightarrow Top View (w.r.t. VP)

Logic: Since the Shape changes from isosceles \blacktriangleright to Equilateral \blacktriangleright in the FV, the plane angle is in the TV. Here plane angle is not given & hence we first draw TS, HL, RS and then IL on the projectors of RS & thus find IL Angle to VP.

Steps:

- 1) In 1st stage, in FV, draw Isosceles \blacktriangleright (TS) $a'b'c'$ of base 50 & altitude 70 at mid of $a'c'$ with starting side vertical & HL abc on xy.
- 2) In 2nd stage, draw RS Equilateral \blacktriangleright of 50 sides at same level as TS. Draw arc of IL abc of same length as HL and project RS to cut IL and hence find the plane angle.
- 3) In 3rd stage Rotate $a_1'c_1'$ at 45° to HP and draw RS. Take projections below & match point to point from IL to get Final Shape $a_1b_1c_1$.



10) Draw a rhombus of diagonals 100 & 60 mm with the longer diagonal horizontal. The figure is the top view of a square of 100 mm long diagonals with a corner on the ground. Draw its front view and find the angle its surface makes with the ground.

Ans) Given data:

- True Shape \longrightarrow Square (d_1 & d_2 100 mm)
- Red Shape \longrightarrow Rhombus (100X60)
- Side/ Corner \longrightarrow Corner (sides @ 45°)
- Shape angle \longrightarrow 90° (d_2 is horizontal)
- Shape Change \longrightarrow Top View
- \implies Plane Angle \longrightarrow FV (w.r.t. HP)

Logic: Since the Shape changes from Square to Rhombus in TV, the plane angle is in the FV. Here plane angle is not given and hence we first draw TS, HL, RS & then IL on the projectors of RS & thus find IL angle to HP (ground).

Steps:

- 1) In 1st stage, in TV, draw a square of 100 mm diagonals (join corners of diagonals to get square) below xy & HL $a'b'c'd'$ on xy.
- 2) In 2nd stage, draw RS Rhombus of 100 & 60 (vertical 100; horizontal 60 mm). Draw arc of IL $a'c'$ of same length as HL and project RS to cut IL in FV & hence find plane angle w.r.t HP (ground).
- 3) In 3rd stage, rotate b-d by 90° to VP & draw RS. Take projections above and match point to point from IL to get Final Shape $a_1'b_1'd_1'$.

