## Unit II: Part 2- Projections of Lines

## Theory Questions

1. What is meant by trace of a line?
A. It is defined as the extension of a given line to the reference plane (HP or VP) to which it is perpendicular or inclined. The line meets the HP or VP as a point. This point is called trace of a line.
2. Explain the terms horizontal trace (HT) and vertical trace (VT) for a line.
A. The point in which the line meets the HP when extended is called HT and the point in which the line meets the VP when extended is called as VT. HT and VT need not lie on HP and VP always. In case of lines inclined to both HP and VP, the HT and VT do not lie always on HP and VP.
3. Explain the method of determining a trace with simple sketches.
A. HT: Consider a line inclined to HP. Extend it to xy to get h. From h, drop a perpendicular on to TV to get HT.


VT: Consider a line inclined to VP. Extend it to $x y$ to get $v$. From $v$, drop a perpendicular on to FV to get VT .

4. When does a line have no traces?
A. (i): When a line is parallel to HP and VP, it has no traces.
(ii) When a line is parallel to HP and inclined to VP, it has only VT and no HT.
(iii) When a line is parallel to VP and inclined to HP, it has only HT and no VT.
(iv) When a line is perpendicular to HP, its HT is its top view and it has no VT.
(v) When a line is perpendicular to VP, its VT is its Front view and it has no HT.
5. When a line is parallel to a plane, its projection on that plane is equal to its
$\qquad$ . (straight line)
6. When a line is perpendicular to a plane, its projection on that plane is a $\qquad$ (Point).
7. (i) If a straight line is inclined to the VP \& is in the HP, what is its front view \& in which projection is the inclination of the line seen?
(ii) If a straight line is inclined to the HP and is in the VP, what is its top view and in which view will the inclination of the line be seen?
A. (i) The front view is a reduced line $\|$ to $x y$ and the inclination of the line is seen in top view.
(ii) The top view is a reduced line $\|$ to $x y$ and the inclination of the line is seen in Front view.
8. The projections of a straight line on to $H P$ \& VP are identical. Describe the position of the straight line \& its projection on to a plane perpendicular to both HP \& VP.
A. (i) The line is parallel to both HP and VP. The projection on the profile plane is a point.
(ii) The line is inclined at complimentary angles to HP and VP (sum of angles $=90^{\circ}$ ). The projection on the profile plane will be the line at true angle to HP and VP.

9. A straight line $A B$ of 40 mm long is contained by a profile plane, end $A$ in $H P$, end $B$ in VP. Draw its projections.

10. When a line is perpendicular to H.P. its $\qquad$ trace will coincide with $\qquad$ view. (HT, TV)
11. When a line is perpendicular to VP, its $\qquad$ trace will coincide with $\qquad$ view. (VT, FV)

## Problems:

## Part-1: Short Answer problems

12. Draw the projections of a straight line $A B$, of 50 mm length for the following positions:
(i) Parallel to \& 20 mm above HP \& on VP.
(ii) Parallel to both HP \& VP \& 20 mm from each.
(iii) Perpendicular to HP, in the VP and its one end is 15 mm above the HP.
(iv) Perpendicular to VP, in the HP and its one end is 15 mm in front of the VP.

13. Draw the projections of a straight line $A B$ of 60 mm length for the following positions:
(i) Inclined to the HP at $35^{\circ}$ and point $A$ is in front of VP at 10 mm and 20 mm above HP.
(ii) Inclined at $60^{\circ}$ to the VP, having one end 20 mm above HP \& 35 mm in front of VP.

14. A line of 100 mm long is parallel to \& 30 mm above HP. Its 2 ends are 25 mm and 50 mm in front of VP respectively. Find its inclinations with the VP.

15. A line $A B$ is 65 mm long and has its end $A$ both in $H P$ and $V P$. It is inclined at $45^{\circ}$ to the HP. Draw its projections.
$a^{\prime} b^{\prime}=65$.

16. A line $\mathrm{PQ}, 50 \mathrm{~mm}$ long has its end P 22 mm from HP and 30 mm from VP. The whole line lies in one quadrant. Draw its projections in anyone of the four quadrants if it is inclined to the HP at $30^{\circ}$ and is parallel to the VP.
$a^{\prime} b^{\prime}=50$.

17. A line $A B, 60 \mathrm{~mm}$ long is parallel to HP \& lies 20 mm above it. The point $A$ is 30 mm \& point $B$ is 60 mm away from the reference axis. Draw the projections $\&$ traces of the line.
$a b=60$.

18. Two pegs fixed on a wall are 4.5 m apart. The distance between the pegs measured one parallel to the floor is 3.6 m . If one peg is 1.5 m above the floor, find the height of the second peg and inclination of the line joining the two pegs, with the floor?

Use scale: 1: 100 ; find $\theta$.

19. A straight line is parallel to both HP and VP. Its one end is 25 mm behind VP and 15 mm above HP. Length of the line is 10 cm . Draw its projections.


Part-2: Long Answer problems
(without data on traces; only location of HT, VT to be shown) (for solutions, refer similar model problems in notes)
20. A line $A B$ is 70 mm long. It is inclined at $45^{\circ}$ to the HP. Its front view a'b' measures 50 mm . The end $A$ is 15 mm above the HP and 20 mm in front of VP. The end $B$ is in the first quadrant. Draw the projections of the line. Determine its inclination with VP and find its traces.
21. $A$ line $A B, 90 \mathrm{~mm}$ long, is inclined at $30^{\circ}$ to the HP. Its end $A$ is 12 mm above HP \& 20 mm in front of VP. Its front view measures 65 mm . Draw the top view of $A B \&$ also find the traces of $A B$.
22. A line $A B$ of 60 mm length is inclined to HP at $45^{\circ}$ \& inclined to $V P$ at $30^{\circ}$ with its end $A$ at 40 mm above $H P \& 50 \mathrm{~mm}$ in front of VP. Draw the projections of the straight line $A B$ \& show its traces.
23. The top view of a 75 mm long line measures 65 mm and its front view measures 50 mm . Its one end is in the HP and 12 mm in front of VP. Draw its projections and find its inclination with HP and VP. Also locate its traces.
24. A line $A B, 90 \mathrm{~mm}$ long, is inclined at $45^{\circ}$ to the HP \& its top view makes an angle of $60^{\circ}$ with the VP. The end $A$ is in the HP \& 12 mm in front of the VP. Draw its front view \& find its true inclination with the VP. Also locate its traces.
25. One end $A$ of a straight line $A B$ is 20 mm above HP and 50 mm before (in front of) VP. The other end $B$ is 70 mm above HP and 25 mm before VP (in front). The distance between the end projectors of the line is 60 mm . Draw the projections of the line and find the true length, true inclinations with HP and VP and the traces of the line.
26. A line $A B 75 \mathrm{~mm}$ long, inclined at $45^{\circ}$ to HP and $30^{\circ}$ to VP . Its end $B$ is in HP and 40 mm in front of VP Draw its projections
27. A line $P O$ is in the first quadrant. Its ends $P$ and 0 are 20 mm and 60 mm in front of the V.P respectively. The distance between the end projectors is 75 mm . The line is inclined at $30^{\circ}$ to the V.P with its end 'P' in H.P. Draw the projections of PO and find its true length and the inclination with the H.P. Also locate its traces HT and VT.

## Part-3: Long Answer problems (with data on traces using HT, VT,etc)

28. The front view of a line $A B$ makes an angle of $30^{\circ}$ with $x y$ line. The $H T$ of the line is 45 mm in front of VP while its VT is 30 mm below the HP. One end of the line $A$ is 12 mm above the $H P \&$ the other end $B$ is 115 mm in front of the VP. Draw the projections of the line \& determine its true length \& its inclinations with HP \& VP. (Refer notes)
29. A line $A B$ is in the $1^{\text {st }}$ quadrant. Its ends $A$ and $B$ are 20 mm and 60 mm in front of $V P$ respectively. The distance between the end projectors is 75 mm . The line is inclined at $30^{\circ}$ to the $H P$ and its $H T$ is 10 mm above $x y$. Draw the projections of $A B$ and find its true length and locate the VT. (Refer notes)
