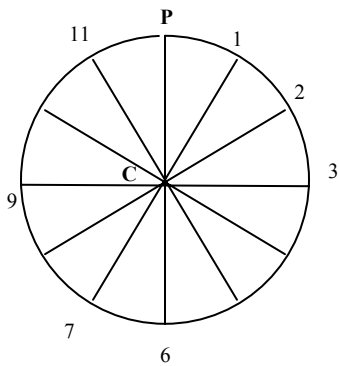


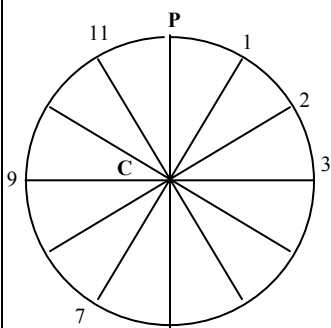
Q) A circle of 50 mm rolls on another circle of 150 mm and inside it. Name the curve. Trace the path of a point P on the circumference of the smaller circle. Also draw a tangent and normal to the curve at a point on the curve, 65 mm from the centre of the bigger circle.

Ans) The **Curve** is a **hypo cycloid** as the **circle** rolls on inside of another circle.
The **angle** for one revolution will be equal to $(360 * d/D)$.

1) Draw a circle of 25 mm radius with centre C and **mark P as the top most point**. Divide the circle into 12 parts and label them as 1, 2, 3...12 after P.



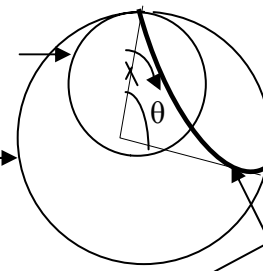
2) From P, mark O, centre of big circle (base circle) at $PO=R=75$ mm.
3) Mark $\angle POA = \theta = 360*(d/D)$ and draw OA at θ from OP.



PO=75; P6=50;
O6=25

R. C (rolling or generating circle) (d)

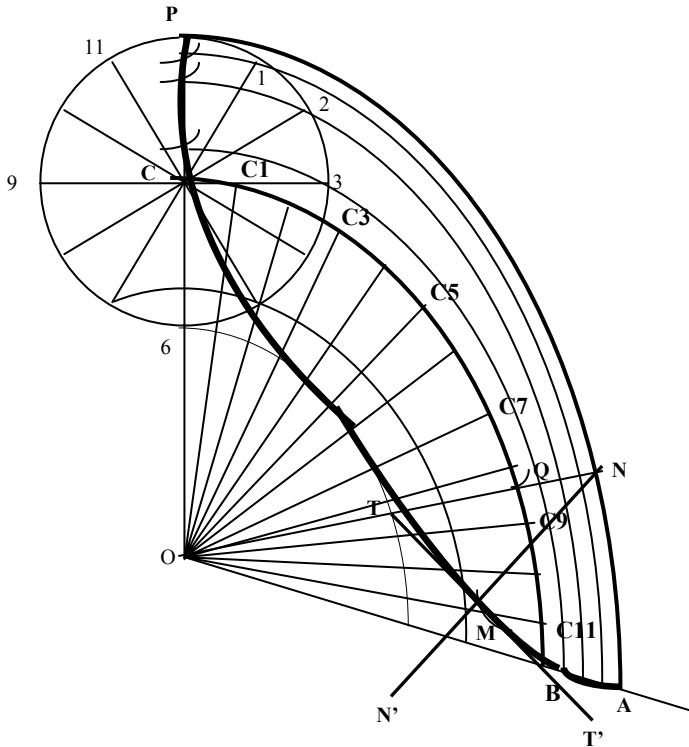
B.C (base or directing circle) (D)



Hypo-Cycloid

The above figure is the profile of the Hypo Cycloid that is generated when the rolling circle of d rolls on a base circle of D and inside it.

- 4) With O as centre and OP radius, draw base circle up to A . PA is part of the base Circle.
- 5) With O as centre and OC radius, draw an arc through centre to get **Centre Arc CB** . On CB , the centers $C_1 \dots C_{12}$ will lie.
- 6) To get the centers, divide $\angle POA$ into 12 equal parts (here $120/12 = 10^\circ$) and join O to each of these 10° on CB to get $C_1, C_2, \dots C_{12}$.



- 7) Now, similar to cycloids, with C_1 centre and radius $CP (=25)$, cut arc on **1-11 arc** of rolling circle to get P_1 . Repeat with C_2, C_3 , etc on 2-10, 3-9, etc to get the hypocycloid.

Note: While dividing the θ into 12 parts, mark centers $C_1, C_2, \dots C_{12}$ on centre arc CB passing through C only and **not** on the arc passing through 3-9.

Arc passing through 3-9 will be separate and is used for getting P_3 and P_9 while cutting arcs.

Tangent and Normal:

- 1) Mark M on the hypocycloid at 65 mm from O by taking O as centre and radius 65.
- 2) With M as center, radius $CP (=25)$, cut arc Q on CB .
- 3) Join QO , extend it to cut base circle PA at N .
- 4) Join NM to get normal NN' , and \perp to NN' draw the tangent TT' .