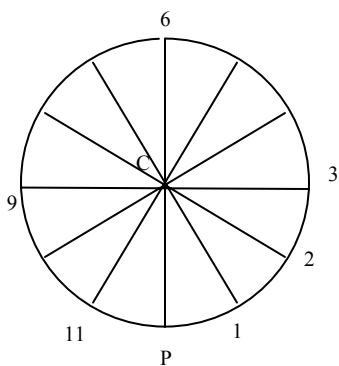


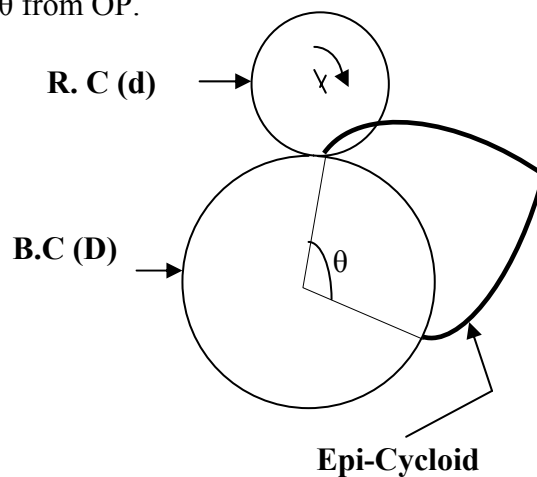
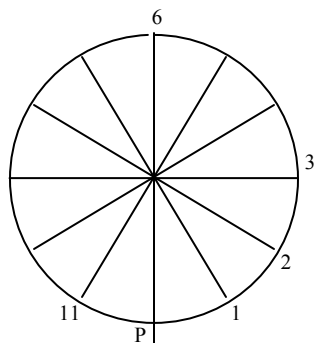
**Q)** A circle of 50 mm rolls on another circle of 150 mm and outside it. Name the curve. Trace the path of a point P on the circumference of the smaller circle. Also draw a tangent and normal to the curve at a point on the curve, 85 mm from the centre of the bigger circle.

**Ans)** The **Curve** is an **epicycloid** as the **circle** rolls on outside of another circle. The **angle** for one revolution will be equal to  $(360 * d/D)$ .

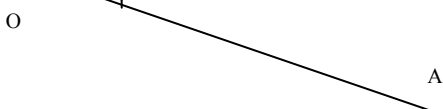
**1)** Draw a circle of 25 mm radius with centre C and mark P as the bottom most point. Divide the circle into 12 parts and label them as 1, 2, 3...12 after P.



**2)** From P, mark O, centre of big circle (base circle) at  $PO=R=75$  mm.  
**3)** Mark  $\angle POA = \theta = 360*(d/D)$  and draw OA at  $\theta$  from OP.

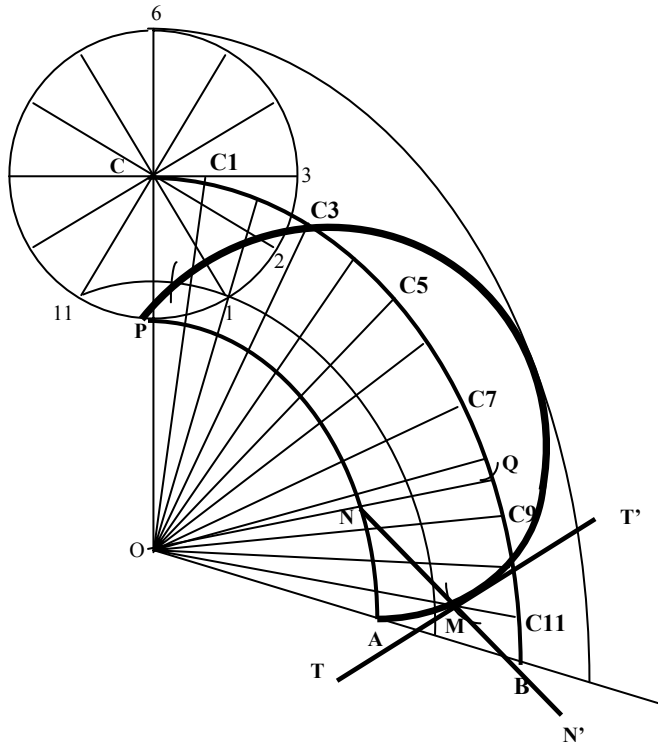


R.C → ROLLING CIRCLE (GENERATING CIRCLE)  
 B.C → BASE CIRCLE (DIRECTING CIRCLE)



The above figure is the profile of the Epi Cycloid that is generated when the rolling circle of  $d$  rolls on a base circle of  $D$ .

- 4) With  $O$  as centre and  $OP$  radius, draw base circle up to  $A$ .  $PA$  is part of the base Circle.
- 5) With  $O$  as centre and  $OC$  radius, draw an arc through centre to get **Centre Arc  $CB$** . On  $CB$ , the centers  $C_1 \dots C_{12}$  will lie.
- 6) To get the centers, divide  $\angle POA$  into 12 equal parts (here  $120/12 = 10^\circ$ ) and join  $O$  to each of these  $10^\circ$  to get  $C_1, C_2, \dots C_{12}$ .



- 7) Now, similar to cycloids, with  **$C_1$  centre and radius  $CP (=25)$** , cut arc on **1-11 arc of rolling circle** to get  $P_1$ . Repeat with  $C_2, C_3$ , etc on 2-10, 3-9, etc to get the epicycloid.

**Note:** While dividing the  $\theta$  into 12 parts, mark centers  $C_1, C_2, \dots C_{12}$  on centre arc  **$CB$**  passing through  $C$  only and **not on the arc passing through 3-9**.

**Arc passing through 3-9** will be **separate** and is used for getting  $P_3$  and  $P_9$  while cutting arcs.

**Tangent and Normal:**

- 1) Mark  $M$  on the epicycloid at 85 mm from  $O$  by taking  $O$  as centre and radius 85.
- 2) With  $M$  as center, radius  $CP (=25)$ , cut arc  $Q$  on  $CB$ .
- 3) Join  $QO$ , cutting base circle  $PA$  at  $N$ .
- 4) Join  $NM$  to get normal  $NN'$ , and  $\perp$  to  $NN'$  draw the tangent  $TT'$ .