

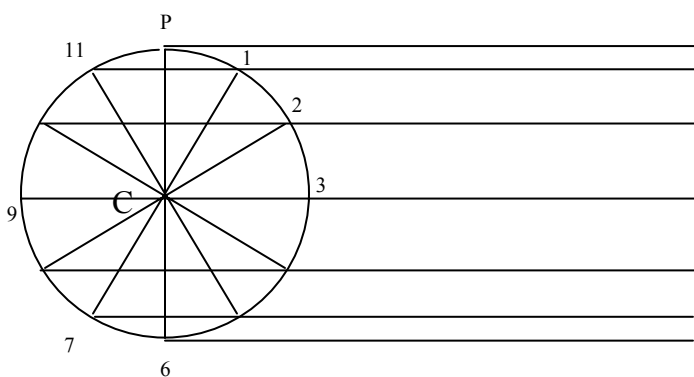
Q) A circle of 50 mm rolls on a horizontal straight line for half revolution. For another half revolution it rolls on a line inclined at 60° to the horizontal. Trace the path of a point P on the circumference of the circle. Take the generating point as top most point of circle.

Ans) The **Curve** is a **cycloid** as the **circle** rolls along a **straight line** without slipping. The **length** for one revolution will be equal to $\pi * D$ (i.e. $3.14 * \text{Diameter of circle}$).

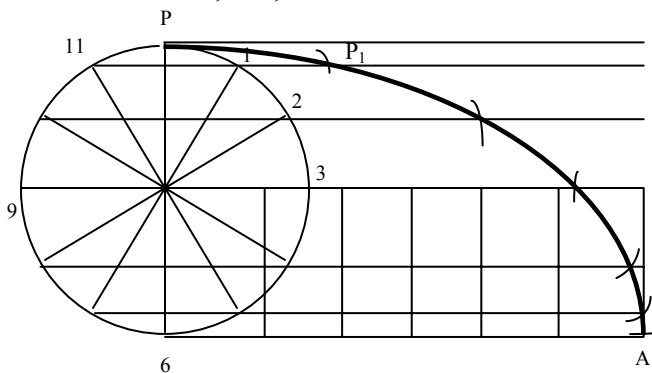
$$L = \pi D = 3.14 * 50 = 157\text{mm.}$$

Since there are 2 half revolutions, the length for each $\frac{1}{2}$ revolution will be $= (\pi * D) / 2$.

1) Draw a circle of 25 mm radius with centre C and mark P as the top most point. Divide the circle into 12 parts and label them as 1, 2, 3...12 after P.



2) At 6, draw a tangent 6A (straight line) length for **half** revolution will be equal to $(\pi * D) / 2$ (i.e. $\pi D / 2 = 78.5$ mm). Divide 6A into 6 equal parts and mark $1', 2', \dots, 6'$. On $1', 2', \dots, 6'$ draw lines \perp to 6A to cut center line CB at C_1, C_2, \dots, C_6 .



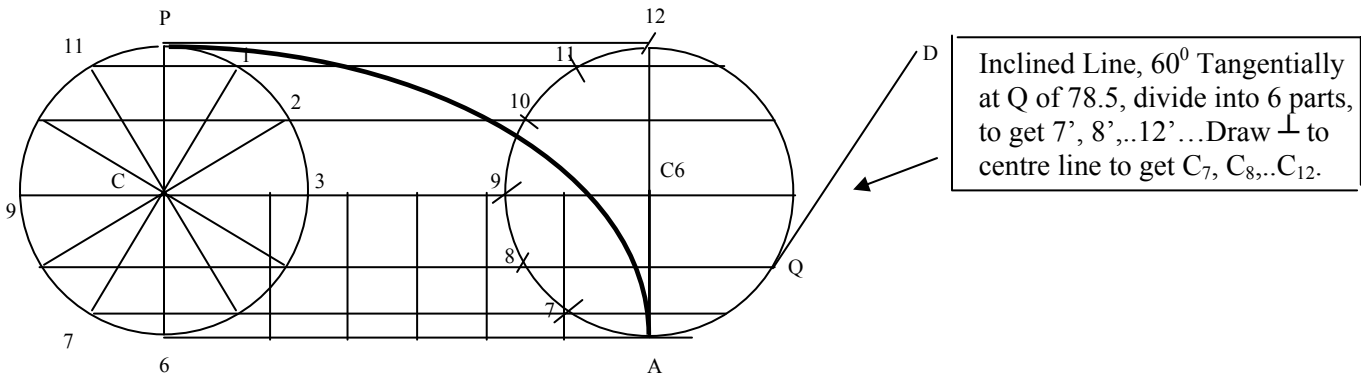
3) With C_1 as centre and $CP (=25)$ as radius, cut arc on 1-11 line of circle to the right side to get first point P_1 . Similarly, repeat with CP radius and C_2, C_3, \dots, C_6 to get **half cycloid**. The steps are similar like earlier cycloids, but P is at top and next points after P are labeled as 1,2,3...12.

The above figure is the completed cycloid for first $\frac{1}{2}$ revolution.

Since there are 2 half revolutions, the length for each $\frac{1}{2}$ revolution will be $= (\pi * D)/2$.

- 4) For the 2nd half revolution, the length of line will be $= (\pi * D)/2 = 78.5$ mm.
Draw the same circle at C_6 with radius = CP (25), with C_6 as centre.

The line should be tangential to circle when it rolls and hence draw inclined line of 78.5mm from Q at 60° with horizontal. Mark 7, 8, 9..12 from A on 2nd circle. On 7,8,9..12, draw lines \parallel to QD (inclined base line of 60°)



- 5) For 2nd half cycloid, start with C_7 as centre, CP radius, cut arc on 7-11 line of 2nd circle. Similarly for C_8, C_9 , etc, get the other points of cycloid.

Note: For 7,8,9 arcs to be cut on left side of centers and for 10, 11 and 12 arcs to be cut on the right side of centers. Last arc will cut 6-12 line on extended lines beyond C_{12}

